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# Wide-range wavelength-tunable photon-pair source for characterizing single-photon detectors

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**Abstract:** The temporal response of single-photon detectors is usually obtained by measuring their impulse response to short-pulsed laser sources. In this work, we present an alternative approach using time-correlated photon pairs generated in spontaneous parametric down-conversion (SPDC). By measuring the cross-correlation between the detection times recorded with an unknown and a reference photodetector, the temporal response function of the unknown detector can be extracted. Changing the critical phase-matching conditions of the SPDC process provides a wavelength-tunable source of photon pairs. We demonstrate a continuous wavelength-tunability from 526 nm to 661 nm for one photon of the pair, and 1050 nm to 1760 nm for the other photon. The source allows, in principle, to access an even wider wavelength range by simply changing the pump laser of the SPDC-based source. As an initial demonstration, we characterize single photon avalanche detectors sensitive to the two distinct wavelength bands, one based on Silicon, the other based on Indium Gallium Arsenide.

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## 1. Introduction

Characterizing the temporal response function of single-photon detectors is crucial in time-resolved measurements, e.g. determining the lifetime of fluorescence markers [1], characterizing the spontaneous decay of single-photon emitters [2] and the photon statistics of astronomical sources [3] and measuring the joint spectral of photon-pair sources [4], so that the timing uncertainty contributed by the detection process can be taken into account. Typically, the temporal response of a detector is obtained from the arrival time distribution of photons collected from a pulsed laser. In this work, we present an alternative approach that leverages on the tight timing correlation [5] of photon pairs generated in spontaneous parametric down-conversion [6,7] (SPDC): the coincidence signature corresponding to the detection of two photons of the same pair is used to infer the temporal response function of the photodetectors. Compared to a pulsed laser, a SPDC source is easier to align, and is wavelength-tunable by changing the critical phase-matching condition of the SPDC process [8]. In addition, one can address two wavelength bands with the same source by choosing a non-degenerate phase matching condition.

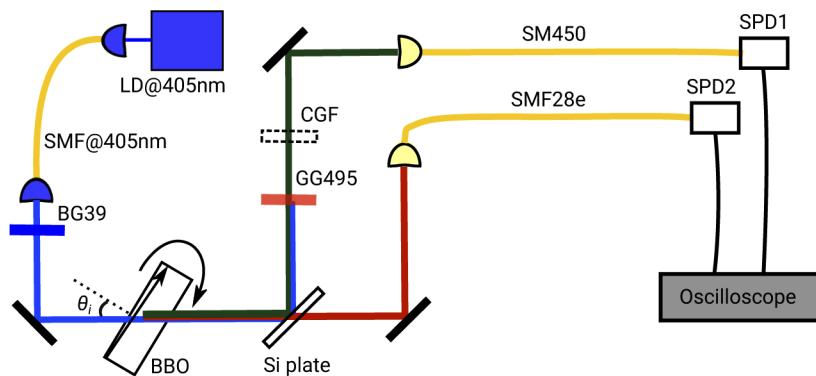
For an initial demonstration, we generate photon pairs with a tunable wavelength range over 100 nm in the visible band, and over 700 nm in the telecommunication band – a tunability at least comparable to existing femtosecond pulsed lasers – and use it to characterize both Silicon (Si-APDs) and Indium Gallium Arsenide (InGaAs-APDs) avalanche photodiodes. In particular, we characterize the timing behaviour of a fast commercial Si-APD (Micro Photon Devices PD-050-CTC-FC) over a continuous wavelength range, for which we previously assumed an approximately uniform temporal response of the detector in the wavelength range from 570 nm to 810 nm [3]. With the measurement reported in this work, we observe a significant variation of

52 the timing jitter even on a relatively small wavelength interval of  $\approx 10$  nm. A better knowledge of  
 53 the timing response of this particular Si APD contributes to a better understanding of coherence  
 54 properties of light in such experiments. Similarly, better characterization of the timing response  
 55 over a wide wavelength range helps to better model fluorescence measurements regularly carried  
 56 out with such detectors [1].  
 57

## 58 2. Correlated photon pair source

59 The basic configuration of the spontaneous parametric down conversion source is shown in Fig. 1.  
 60 The output of a laser diode (central wavelength  $\lambda_p = 405$  nm, output power 10 mW) is coupled  
 61 to a single-mode optical fiber for spatial mode filtering, and focused to a Gaussian beam waist  
 62 of  $70 \mu\text{m}$  into a 2 mm thick  $\beta$ -Barium Borate crystal as the nonlinear optical element, cut for  
 63 Type-II phase matching ( $\theta_0 = 43.6^\circ$ ,  $\phi = 30^\circ$ ).  
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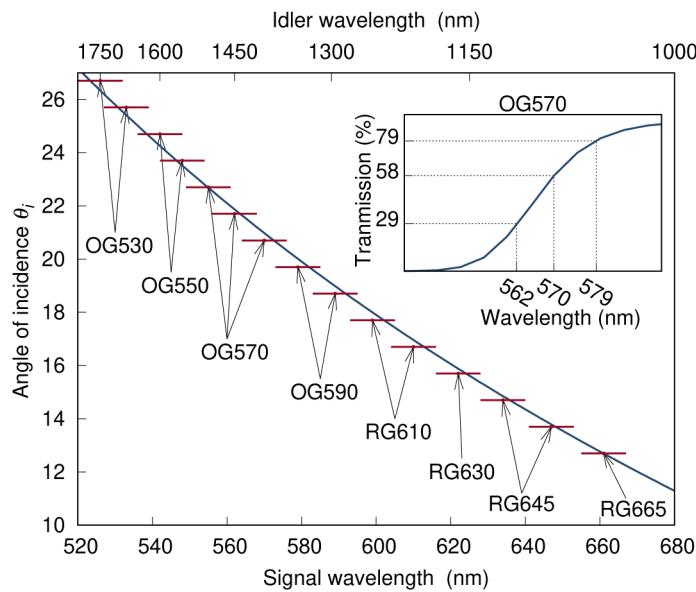
65 For this cut, SPDC generates photon pairs in the visible and telecommunications band,  
 66 respectively. We collect the photons in a collinear geometry, with collection modes (beam waists  
 67  $\approx 50 \mu\text{m}$ ) defined by two single-mode fibers: one fiber (SMF450: single mode from 488 nm to  
 68 633 nm) collects signal photons and delivers them to the single-photon detector SPD1, while  
 69 the other fiber (standard SMF28e, single transverse mode from 1260 nm to 1625 nm) collects  
 70 idler photons and delivers them to SPD2. The signal and idler photons are separated to their  
 71 respective fibers using a  $100 \mu\text{m}$ -thick, polished Silicon (Si) plate as a dichroic element. The  
 72 plate acts as a longpass filter (cut-off wavelength  $\approx 1.05 \mu\text{m}$ ), transmitting only the idler photons  
 73 while reflecting approximately half of the signal photons.  
 74



87 **Fig. 1.** Wavelength-tunable photon pair source based on Type-II SPDC. The critical  
 88 phase-matching condition is changed by varying the angle of incidence  $\theta_i$  of the pump at  
 89 the crystal, in order to generate photon pairs at the desired wavelength in the visible and  
 90 telecommunications band. A Silicon (Si) plate separates the photons in each pair. Tight  
 91 timing correlations between photons in each pair, and a characterized detector SPD2, allow  
 92 measuring the jitter of a single-photon detector (SPD1). A calibrated color glass filter (CGF)  
 93 can be inserted to infer the wavelength of the photons sent to SPD1 using a transmission  
 94 measurement. LD: laser diode, BBO:  $\beta$ -Barium Borate, SMF: single-mode fiber, GG495,  
 95 BG39: color glass filters.

96 To suppress uncorrelated visible and infrared photons detected by our SPDs, we insert both a  
 97 blue color glass bandpass filter (BG39) in the pump path, attenuating parasitic emission from the  
 98 pump laser diode and broadband fluorescence from the mode cleaning fiber, and a green color  
 99 glass longpass filter (GG495) in the path of the idler photons to suppress pump light at SPD1.  
 100 For the idler path, the silicon dichroic is sufficient. To tune the wavelength of down-converted  
 101 photons, we change the critical phase-matching condition of the SPDC process by varying the  
 102 angle of incidence  $\theta_i$  of the pump beam at the crystal [9,10]. Figure 2 (red dots) shows the signal

103 and idler wavelengths,  $\lambda_s$  and  $\lambda_i$ , measured for our source for  $\theta = 12.7^\circ$  to  $26.7^\circ$ . To measure the  
 104 signal wavelength  $\lambda_s$ , we insert different standardized color glass longpass filters (CGF in Fig. 1)  
 105 for different angles  $\theta_i$ , and measure the transmission of the signal photons in order to infer their  
 106 wavelength. The inset of Fig. 2 shows an example where a filter OG570 is used to infer  $\lambda_s$  close  
 107 to the cut-off wavelength of the filter. The corresponding idler wavelength is calculated through  
 108 energy conservation in SPDC,  $\lambda_i^{-1} = \lambda_p^{-1} - \lambda_s^{-1}$ . Our measured SPDC wavelengths can be well  
 109 described by a numerical phase matching model based on optical dispersion properties of BBO  
 110 [11,12] (blue line).  
 111



131 **Fig. 2.** Signal ( $\lambda_s$ ) and idler ( $\lambda_i$ ) wavelength dependence on the angle of incidence  $\theta_i$  of the  
 132 pump beam at the  $\beta$ -BBO crystal, produced in Type-II SPDC. We obtain  $\lambda_s$  by measuring  
 133 the transmission of signal photons through a set of calibrated color glass filters (OGs and  
 134 RGs).  $\lambda_i$  is calculated from  $\lambda_s$  by the law of energy conservation. Error bars: uncertainty of  
 135 the central transmission wavelength of the filters. Solid line: model predicting the output  
 136 wavelengths based on energy and momentum conservation laws governing SPDC. Inset: the  
 137 transmission-wavelength calibration curve of color glass filter OG570 used to experimentally  
 138 determine three values of  $\lambda_s$ .

139 This simple pair source provides photons in a wavelength range of  $\lambda_s = 526$  nm to  $661$  nm  
 140 and  $\lambda_i = 1050$  nm to  $1760$  nm, comparable with existing dye and solid-state femtosecond pulsed  
 141 lasers [13,14]. In the following section, we demonstrate how the tight timing correlations of each  
 142 photon pair can be utilized to characterize the temporal response of single photon detectors.  
 143

### 144 3. Characterizing the temporal response of single-photon detectors

145 The time response function  $f(t)$  of a single photon detector characterizes the distribution of signal  
 146 events at a time  $t$  after a photon (of a sufficiently short duration) is absorbed by a detector. It  
 147 characterizes the physical mechanism that converts a single excitation into a macroscopic signal,  
 148 and can be measured e.g. recording the average response to attenuated optical pulses from a  
 149 femtosecond laser [15]. In this paper, we use the timing correlation in a photon pair, which  
 150 emerges at an unpredictable point in time. This requires two single photon detectors registering a  
 151 photon. As the photon pair is correlated on a time scale of femtoseconds, and the relevant time  
 152 scales for detector responses is orders of magnitudes larger, the correlation function  $c_{12}(\Delta t)$  of  
 153

154 time differences  $\Delta t$  between the macroscopic photodetector signals is a convolution of the two  
 155 detector response functions,  
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$$157 \quad c_{12}(\Delta t) = N(f_1 * f_2)(\Delta t) = N \int f_1(t)f_2(\Delta t - t)dt, \quad (1)$$

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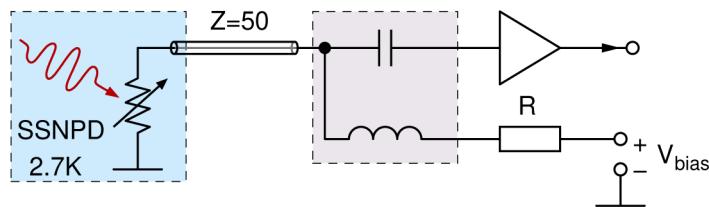
159 where  $N$  the total number of recorded coincidence events. Obtaining the detector response  
 160 function  $f_1(t)$  from a measured correlation function  $c_{12}(\Delta t)$  requires the known response function  
 161  $f_2(t)$  of a reference detector. For a device under test,  $f_1(t)$  can then be either reconstructed by  
 162 fitting a  $c_{12}(\Delta t)$  in Eq. (1) with a reasonable model for  $f_1(t; P)$  (with a parameter set  $P$ ) to a  
 163 measured correlation function, or obtained from it via deconvolution.  
 164

165 To measure  $c_{12}(\Delta t)$ , we evaluate the detection time at single photon detector SPD1 by recording  
 166 the analog detector signal with an oscilloscope, and interpolating the time it crosses a threshold  
 167 of around half the average signal height with respect to a trigger event caused by a signal of  
 168 single photon detector SPD2. The histogram of all time differences  $\Delta t$  for many pair events then  
 169 is a good representation of  $c_{12}(\Delta t)$ .  
 170

#### 4. Reference detector characterization

171 We use a superconducting nanowire detector (SNSPD) with a design wavelength at 1550 nm as  
 172 the reference detector SPD2, because a SNSPD has an intrinsic wide-band sensitivity and fast  
 173 temporal response. To determine its response function  $f_2(t)$ , we measure the correlation function  
 174  $c_{12}$  from photon pairs with two detectors of the same model (Single Quantum SSPD-1550Ag).  
 175

176 Figure 3 shows the biasing and readout circuit of a single SNSPD. The SNSPD is kept at  
 177 a temperature of 2.7 K in a cryostat, and is current-biased using a constant voltage source  
 178 ( $V_{bias} = 1.75$  V) and a series resistor ( $R = 100$  k $\Omega$ ) through a bias-tee at room temperature. The  
 179 signal gets further amplified by 40 dB at room temperature to a peak amplitude of about 350 mV.  
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 188 **Fig. 3.** Biasing and readout circuit for the superconducting nanowire single-photon detector  
 189 (SNSPD). The SNSPD is current-biased using a constant voltage source and a series resistor  
 190  $R$ . When a photon is absorbed by the SNSPD, it changes temporarily from a superconducting  
 191 to a conducting state. The resulting current change reaches a signal amplifier, which provides  
 192 the photodetection signal.

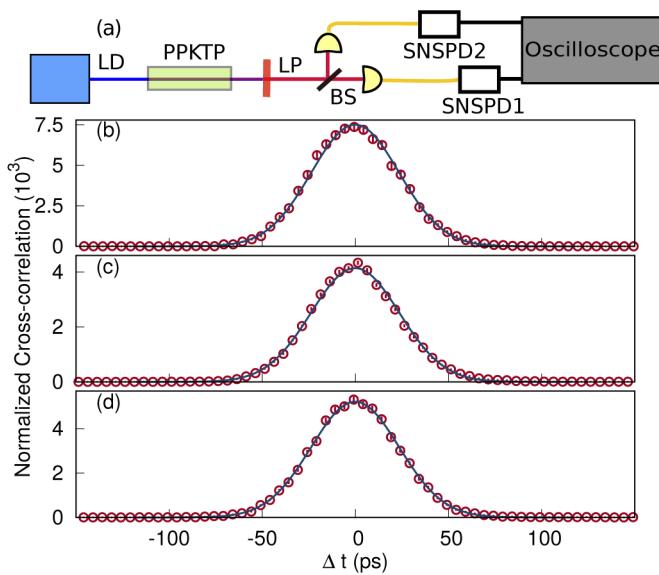
193 We first expose both detectors to photons at a wavelength of 810 nm using a degenerate  
 194 PPKTP-based photon pair source pumped with a 405 nm laser diode (Fig. 4 (a)). The choice of  
 195 using this source instead of the BBO-based source shown in Fig. 1 was borne out of convenience  
 196 rather than from any limitation in our BBO-based source described before, as the PPKTP-based  
 197 type-II SPDC source was readily available [16]. Fig. 4 (b) shows the cross-correlation  $c_{12}(\Delta t)$  for  
 198 the two SNSPDs, normalized to background coincidences (red dots).  
 199

200 The histogram closely follows a Gaussian distribution (blue line) with standard deviation  
 201  $\sigma_{12} = 23.6(1)$  ps. This suggests that the two responses  $f_1(t), f_2(t)$  are also Gaussian distributions,  
 202 and Eq. (1) can be simplified to

$$203 \quad c_{12}(\Delta t) = NG(\sigma_{12}, \Delta t) + C_0 = NG(\sigma_1, \Delta t) * G(\sigma_1, \Delta t) + C_0, \quad (2)$$

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**Fig. 4.** (a) Simplified schematic of the PPKTP-based photon-pair source. We generate orthogonally-polarized, degenerate photon pairs at 810 nm using Type-II SPDC, by pumping a PPKTP crystal (9.55  $\mu$ m poling period) with a 405 nm laser beam. The photon pairs are separated by a polarizing beam-splitter and fibre-coupled to two SNSPDs. By changing the pump wavelength to 532 nm, the same crystal generates 810 nm and 1550 nm photon pairs in a Type-0 SPDC process. We use a Si plate as a beam splitter to separate the non-degenerate photon pairs. BS: beam splitter, LD: laser diode, LP: longpass filter, PPKTP: Periodically Poled Potassium titanyl phosphate crystal. Cross-correlation of photodetection times registered by two SNSPDs detecting (b) degenerate 810 nm photon pairs, and (c) non-degenerate photon pairs at 810 nm and 1550 nm from the PPKTP-based source. (d) Cross-correlation of photodetection times of non-degenerate photon pairs at 548 nm and 1550 nm from the BBO-based source in Fig. 1.

236 where  $N$  is the total number of correlated photon pairs detected,  $G(\sigma, \Delta t) = e^{-\Delta t^2/(2\sigma^2)} / \sqrt{2\pi\sigma^2}$   
 237 is a normalized Gaussian distribution, and  $C_0$  is associated with the accidental coincidence rate.  
 238 The standard distribution of the correlation is then simply related to those of the individual  
 239 detectors by  $\sigma_{12}^2 = \sigma_1^2 + \sigma_2^2$ . Assuming the same response for both detectors, we can infer at a  
 240 wavelength of 810 nm, corresponding to a the full-width at half-maximum (FWHM) of 39.2(2) ps.  
 241

242 Next, we calibrate the SNSPD at 1550 nm using photon pairs at 810 nm and 1550 nm generated  
 243 from the same PPKTP-based SPDC source pumped with a 532 nm laser diode [Fig. 4(a)]. The  
 244 non-degenerate photon pairs are separated by a Si plate as a dicroic element. Figure 4(c) shows  
 245 the cross-correlation (red dots) of the photodetection times at the two SNSPDs, and a fit of  
 246 a Gaussian distribution (blue line) with a standard deviation  $\sigma_{12,810/1550} = 23.8(2)$  ps. With  
 247  $\sigma_{1,810} = 16.7(1)$  ps obtained at 810 nm previously, we obtain  $\sigma_{2,1550} = \sqrt{\sigma_{12,810/1550}^2 - \sigma_{1,810}^2}$   
 248 resulting in a timing jitter of 39.9(6) ps (FWHM) of the SNSPD at 1550 nm.

249 Finally, to determine the temporal response function of a SNSPD at 548 nm, we used the  
 250 BBO-based pair source [Fig. 1] to prepare non-degenerate photon pairs at 548 nm and 1550 nm.  
 251 Figure 4(d) shows the cross-correlation obtained with our detectors. The fit to a Gaussian  
 252 distribution (blue line) leads to a standard deviation  $\sigma_{12,548/1500} = 23.7(1)$  ps. With the same  
 253 argument as before, and using  $\sigma_{1,1500} = 16.9(2)$  ps, we obtain a timing jitter of 38.9(7) ps  
 254 (FWHM) at 548 nm. So in summary, the timing jitter of the SNSPD shows no statistically  
 255 significant dependency on the wavelength in our measurements.

256 The timing jitter partially originates from the threshold detection mechanism: for a photo-  
 257 todetection signal  $V(t)$ , the timing uncertainty  $\sigma_t$  for crossing a threshold, contributed by the  
 258 electrical noise  $\sigma_V$ , is given by  $\sigma_{t,\text{noise}} = \sigma_V / (dV/dt)$  at the threshold [17,18]. For our SNSPDs,  
 259 we estimate  $\sigma_{t,\text{noise}} \approx 15$  ps, corresponding to a contribution of about 35 ps to the timing jitter of  
 260 the combined SNSPD and electronic readout system, i.e., we are dominated by this electrical  
 261 noise. The jitter of the oscilloscope is claimed to be a few ps, which suggests that the intrinsic  
 262 jitter of these SNSPDs is about 10 – 20 ps (FWHM) [19].

263 In the following section, we use the standard deviation  $\sigma_2$  obtained at these wavelengths to  
 264 define the temporal response function of the reference detector  $f_2 = G(\sigma_2)$  in Eq. (1), and use the  
 265 method outlined in Sec. 3. to characterize  $f_1$  of an unknown detector.

## 267 5. Avalanche photodetector characterization

268 First, we characterize the temporal response function  $f_{\text{Si}}$  of a thin Silicon avalanche photodiode  
 269 (Si-APD) from Micro Photon Devices (PD-050-CTC-FC). Although thin Si-APDs have been  
 270 characterized in previous works at a few discrete wavelengths [20–22], there has yet been a  
 271 characterization performed over a continuous wavelength range.

272 Following Refs. [3,23], we describe the temporal response function with a heuristic model

$$274 f_{\text{Si}}(\Delta t) = A G(\sigma, \Delta t - \mu) + B G(\sigma, \Delta t - \mu) * e^{-(\Delta t - \mu)/\tau}, \quad (3)$$

276 a combination of a Gaussian component of mean  $\mu$  and standard deviation  $\sigma$ , and an exponential  
 277 term with a characteristic decay constant  $\tau$ . The weights of each distribution are described by  $A$   
 278 and  $B$ . The Gaussian component is associated with an avalanche that occurs due to the absorption  
 279 of a photon in the depletion region. The exponential component, convoluted with a Gaussian  
 280 distribution, is associated with an avalanche that is initiated by a photoelectron that diffused into  
 281 the depletion region produced by photon absorption elsewhere.

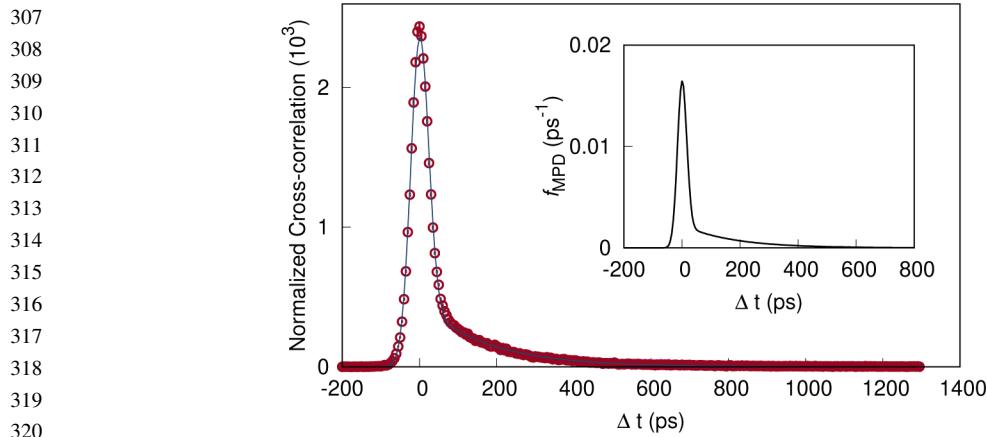
282 We characterize the Si-APD over a wavelength range from  $\lambda_1 = 542$  nm to 647 nm in steps  
 283 of about 10 nm. The photon wavelength is tuned by rotating the crystal, changing the angle  
 284 of incidence  $\theta_i$  of the pump from  $13.7^\circ$  to  $24.7^\circ$ , in steps of  $1^\circ$ . For each  $\theta_i$ , we obtain the  
 285 cross-correlation  $c_{12}(\Delta t)$  similarly as in section 4. Figure 5 (red dots) shows  $g^{(2)}$ , the cross-  
 286 correlation normalized to background coincidences, obtained when signal and idler wavelengths  
 287 are  $\lambda_1 = 555$  nm and  $\lambda_2 = 1500$  nm, respectively. For every  $(\theta_i, \lambda_1, \lambda_2)$ , we deduce  $f_{\text{Si}}$  by fitting  
 288 the measured  $c_{12}$  to the model in Eq. (1) with  $f_1 = f_{\text{Si}}$ , and  $f_2$  a Gaussian distribution with  
 289 full-width at half-maximum (39.9 ps) corresponding to the SNSPD jitter at 1550 nm. For the  
 290 SNSPD, we assume that its jitter remains constant over the wavelength range  $\lambda_2 = 1082$  nm  
 291 to 1602 nm, motivated by the observation that it does not differ significantly for  $\lambda_2 = 810$  nm  
 292 and 1550 nm. The fit results in parameters  $\sigma$  and  $\tau$  which characterize  $f_{\text{Si}}$  at the corresponding  
 293 wavelength  $\lambda_1$ . Figure 5 (inset) shows  $f_{\text{Si}}(\Delta t)$  for  $\lambda_1 = 555$  nm.

294 Two figures of merit are of interest for characterizing the thin Si APD: the duration  $\tau$  of the  
 295 exponential tail, and the ratio  $R$  between the coincidences attributed to the Gaussian component  
 296 to those attributed to the exponential component,

$$297 R = \frac{\int_{-\infty}^{\infty} A G(\sigma, \Delta t - \mu)}{\int_{-\infty}^{\infty} B G(\sigma, \Delta t - \mu) * e^{-(\Delta t - \mu)/\tau}} = \frac{A}{B\tau}. \quad (4)$$

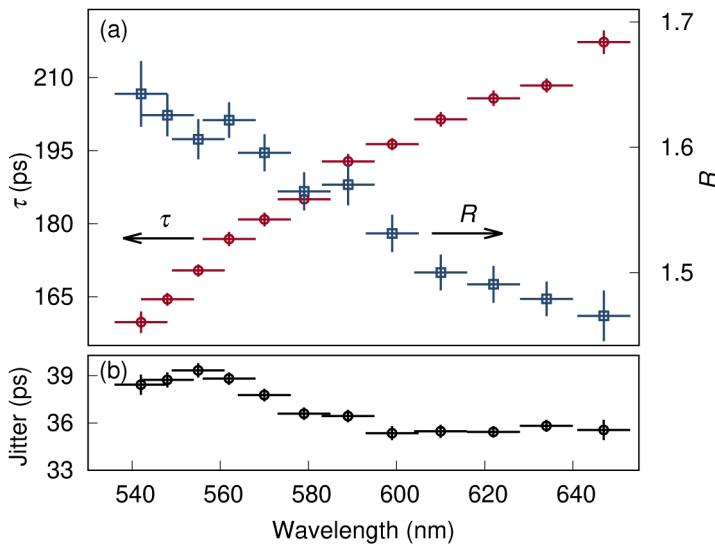
301 Both values determine if the full-width at half-maximum (FWHM), a value typically quoted  
 302 for the detector jitter, serves as a good figure of merit for the temporal response of a detector.  
 303 For example, the jitter of a detector with  $R \ll 0.5$  and  $\sigma \ll \tau$ , is better described by  $\tau$  than the  
 304 FWHM of the temporal response function.

305 Figure 6 (a) shows that  $R$  reduces while  $\tau$  increases with increasing wavelength. The detector  
 306 jitter (FWHM) is shown in Fig. 6 (b). The observation that  $\tau$  changes significantly with wavelength



**Fig. 5.** Cross-correlation between photodetection times at a Si-APD and a characterized SNSPD, normalized to background coincidences  $g^{(2)}(\Delta t)$ . The detectors were illuminated by a non-degenerate (555 nm, 1500 nm) photon pair source. By fitting the data (red dots) to a model (blue line) obtained by convolving the individual temporal response model of both detectors, we are able to extract parameters describing the temporal response of the Si-APD (inset).  $\Delta t$ : photodetection time difference.

is especially relevant for fluorescence lifetime measurements, where the exponential tail in the temporal response function can be easily misattributed to fluorescence when the detector is not characterized at the wavelength of interest [1].



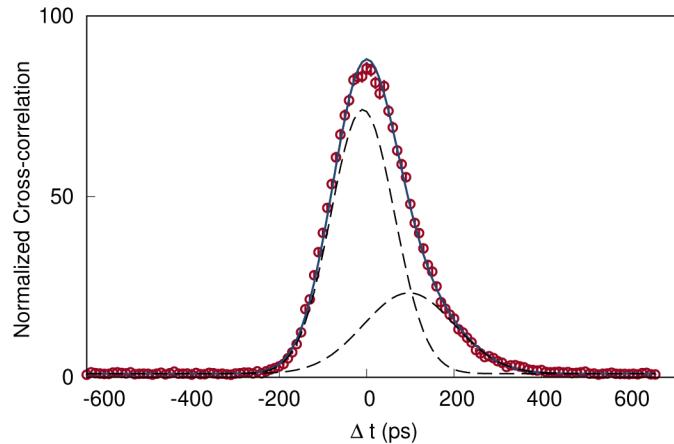
**Fig. 6.** (a) Si-APD temporal response characteristics: ratio  $R$  between the Gaussian and the exponential component of the temporal response function (red), and characteristic decay constant  $\tau$  of the exponential component (blue). (b) Measured timing jitter of a Si-APD as a function of wavelength. Horizontal error bars: uncertainty of the cut-off wavelength of the color glass filter used to measure photon wavelength. Vertical error bars: fit error of  $R$ ,  $\tau$ , and timing jitter.

358 Next, we characterize the temporal response function  $f_{\text{InGaAs}}$  of an InGaAs avalanche photodiode  
 359 (S-Fifteen Instruments ISPD1) which is sensitive in the telecommunication band. We extract  
 360  $f_{\text{InGaAs}}$  by measuring the cross-correlation  $c_{12}$  of the detection times between the InGaAs-APD  
 361 and our reference SNSPD. We note that since the expected jitter of the InGaAs-APD ( $\approx 200$  ps)  
 362 is significantly larger than that of the SNSPD ( $\approx 40$  ps),  $f_{\text{InGaAs}}$  is well-approximated by  $c_{12}$ .

363 Again, we fit  $c_{12}(\Delta t)$  to a heuristic model [24], here comprising of a linear combination of two  
 364 Gaussian distributions

$$366 c_{12}(\Delta t) \approx N f_{\text{InGaAs}}(\Delta t) + C_0 = N[A G(\mu_1, \sigma_1, \Delta t) + B G(\mu_2, \sigma_2, \Delta t)] + C_0, \quad (5)$$

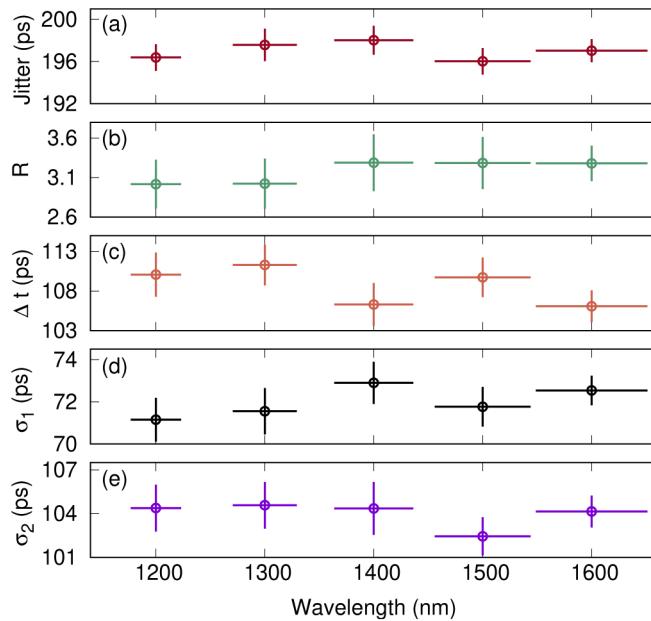
367 where  $A$  and  $B$  are the weights of each distribution,  $\mu_1$  ( $\mu_2$ ) and  $\sigma_1$  ( $\sigma_2$ ) is the mean and standard  
 368 deviation characterizing the Gaussian distribution  $G$ , and  $C_0$  is associated with the accidental  
 369 coincidence rate. Figure 7 shows the measured cross-correlation  $c_{12}$  (red dots) and the fit result  
 370 (blue line) when the InGaAs-APD detected photons with a wavelength of 1200 nm.



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 387 **Fig. 7.** Cross-correlation function normalized to background coincidences  $g^{(2)}(\Delta t)$  of the  
 388 InGaAs-APD and the reference SNSPD. The cross-correlation approximates the InGaAs-  
 389 APD temporal response well since the latter is much slower than the SNSPD. We fit the  
 390 measured  $g^{(2)}(\Delta t)$  (red dots) with a model consisting of two Gaussian distributions (solid line)  
 391 with an overall width of 196 ps (FWHM). Dashed lines: individual Gaussian components,  
 392  $\Delta t$ : time difference between the photodetection times.

393 We tune the wavelength of the photons sent to the InGaAs-APD from 1200 nm to 1600 nm  
 394 in steps of 100 nm, and obtain  $c_{12}$  for each wavelength. Figure 8 shows the parameters  
 395 describing the temporal response of the InGaAs-APD: its jitter, the ratio  $R = A/B$  of the two  
 396 Gaussian distributions contributing to  $f_{\text{InGaAs}}$ , the temporal separation between the two Gaussian  
 397 distributions ( $\mu_1 - \mu_2$ ), and the standard deviation of the two Gaussian distributions ( $\sigma_1, \sigma_2$ ). We  
 398 find no significant variation of any parameter over the entire wavelength range.

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**Fig. 8.** Parameters describing the temporal response function  $f_{\text{InGaAs}}$  of an InGaAs-APD, measured over a wide wavelength range for a linear combination of two Gaussian distributions to model  $f_{\text{InGaAs}}$  (Eq. (5)). The parameters are extracted by fitting the measured temporal response to this model: (a) timing jitter, (b) the weight ratio  $R$  of the Gaussian distributions, (c) the temporal separation  $\mu_1 - \mu_2$  between the Gaussian distributions, (d) and (e) the standard deviations  $\sigma_1$  and  $\sigma_2$  of the Gaussian distributions.

## 6. Conclusion

We have presented a widely-tunable, non-degenerate photon-pair source that produces signal photons in the visible band, and idler photons in the telecommunications band. With the source, we demonstrate how the tight-timing correlations within each photon pair can be utilized to characterize single-photon detectors. This is achieved by measuring the cross-correlation of the detection times registered by the device-under-test (DUT), and a reference detector – an SNSPD, which has a relatively low and constant jitter over the wavelength range of interest. By taking into account the jitter introduced by the reference detector, we are able to extract the temporal response function of the DUT. As the source is based on SPDC in a BBO crystal, its output wavelengths are continuously tunable by varying the angle of incidence of the pump at the crystal. We experimentally demonstrated wavelength-tunability of over 100 nm in the visible band, and over 700 nm in the telecommunications band – a similar tunability compared to existing femtosecond pulsed laser systems.

With our source, we measured the temporal response functions of two single-photon detectors, an Si-APD and an InGaAs-APD, over a continuous wavelength range centered at the visible and telecommunications band, respectively. For the InGaAs-APD, we observed no significant variation of its jitter over a wide wavelength range. For the Si-APD, we observed that the exponential component of its temporal response increases with wavelength. This observation emphasizes the need for an accurate accounting of Si-APD jitter in precision measurements, e.g. characterizing fluorescence markers at the wavelength of interest [1], or measuring the photon statistics of narrowband astronomical sources [3].

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