





Laboratory Demonstration of Spatial Linear Dark Field Control For Imaging Extrasolar Planets in Reflected Light

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Abstract

Imaging planets in reflected light, a key focus of future NASA missions and extremely large telescopes, requires advanced wavefront control to maintain a deep, temporally correlated null of stellar halo—i.e., a dark hole (DH)—at just several diffraction beam widths. Using the Ames Coronagraph Experiment testbed, we present the first laboratory tests of Spatial Linear Dark Field Control (LDFC) approaching raw contrasts ($\sim 5 \times 10^{-7}$) and separations ($1.5\text{--}5.2\lambda/D$) needed to image Jovian planets around Sun-like stars with space-borne coronagraphs like WFIRST-CGI and image exo-Earths around low-mass stars with future ground-based 30 m class telescopes. In four separate experiments and for a range of different perturbations, LDFC largely restores (to within a factor of 1.2–1.7) and maintains a DH whose contrast is degraded by phase errors by an order of magnitude. Our implementation of classical speckle nulling requires a factor of 2–5 more iterations and 20–50 deformable mirror (DM) commands to reach contrasts obtained by spatial LDFC. Our results provide a promising path forward to maintaining DHs without relying on DM probing and in the low-flux regime, which may improve the duty cycle of high-contrast imaging instruments, increase the temporal correlation of speckles, and thus enhance our ability to image true solar system analogues in the next two decades.

Key words: Astronomical instrumentation – Exoplanet detection methods – Exoplanets

Online material: color figures

1. Introduction

Over the past decade, ground-based telescopes using facility adaptive optics (AO) systems and now dedicated *extreme* AO systems have provided the first direct images of self-luminous, (super-)Jovian mass planets orbiting young stars (e.g., Marois et al. 2008; Lagrange et al. 2010; Rameau et al. 2013; Currie et al. 2014, 2015; Macintosh et al. 2015; Chauvin et al. 2017; Keppler et al. 2018). Follow-up multi-wavelength photometry and spectroscopy (Currie et al. 2011; Barman et al. 2015; Rajan et al. 2017) have yielded the first constraints on their atmospheric properties, such as clouds, chemistry and surface

gravity. The soon-to-be launched James Webb Space Telescope may provide the first direct images of self-luminous (super-) Jovian exoplanets around intermediate-aged stars and will prove a unique probe of atmospheric chemistry and the properties of dust entrained in exoplanets' clouds (e.g., Beichman et al. 2010).

Imaging exoplanets in reflected light from future space missions or ground-based extreme AO systems requires new advances in wavefront control (WFC) and coronagraphy (e.g., Guyon 2018; Crill et al. 2019). High-contrast imaging testbeds utilizing focal plane WFC techniques like speckle nulling (Malbet et al. 1995; Bordé & Traub 2006) and electric field conjugation (EFC;

Give'on et al. 2007) and advanced coronagraphy can generate deep dark holes (DH) around a star at the 10^{-8} level in air and 10^{-9} or lower in vacuum (e.g., Belikov et al. 2011, 2012; Trauger et al. 2011; Cady et al. 2016). On ground-based telescopes, wavefront sensing and control advances (e.g., Zernike phase sensing and predictive control) have shown promise on new, state-of-the-art extreme AO systems like SCEXAO and could yield orders of magnitude gain in raw contrast (N'Diaye et al. 2013, 2016; Males & Guyon 2018; Males et al. 2018; Currie et al. 2019a).

Achieved null depths in monochromatic light and narrow bandpasses ($\lesssim 10^{-8}$ – 10^{-9}) are, *if sustained*, sufficient to image reflected-light Jovian planets orbiting at 1–5 au from space telescopes, even around obscured apertures like WFIRST-CGI (Seo et al. 2018; Shi et al. 2018). On the ground, upcoming extremely large telescopes (ELTs) delivering sustained contrasts of $\sim 10^{-6}$ and temporally correlated residual speckles *could* enable reflected-light imaging of numerous Jovian planets, even perhaps Earth-like planets around the nearest low-mass stars. (e.g., Guyon et al. 2018; Lopez-Morales et al. 2019).

Sustaining deep contrasts within a DH necessary to image planets in reflected light imposes significant demands on wavefront sensing, as the residual stellar halo must be measured with extreme precision. Precision sensing is particularly difficult when the DH itself is used for focal-plane WFC (FPWFC) and is already photon starved, as can be the case for standard methods like EFC and speckle nulling. Furthermore, by modulating the deformable mirror (DM) to determine and update an estimate of the electric field, FPWFC methods like EFC can perturb science exposures and thus limit an observation's duty cycle. Instead of using the science target for FPWFC itself, another strategy (for WFIRST CGI) is to first dig a DH around a far brighter reference star within 15° – 20° of a science target and then apply the high-order DM correction to the science target (Bailey et al. 2018). However, both the average contrast of the DH and its temporal correlation with respect to its initial state can and likely will degrade due to any number of dynamic aberrations. Slewing back to the reference star to rebuild the DH, as is currently baselined for WFIRST-CGI, substantially increases an observation's duty cycle. Advanced post-processing methods can yield substantial contrast gains (a factor of ~ 100) (e.g., Soummer et al. 2011; Currie et al. 2012). But the brightening of the DH and its decorrelation over time degrades the effectiveness of these post-processing methods to remove residual starlight impeding planet detection.

Linear Dark Field Control (LDFC) is a promising WFC method which could maintain a static, deep DH without deformable mirror probing after the DH's creation from FPWFC methods (Miller et al. 2017). LDFC utilizes the linear response of the uncorrected but photon-rich region in the focal plane (the “bright field” or BF) to wavefront perturbations that affect both the BF and the photon-starved DF.¹⁷ Because

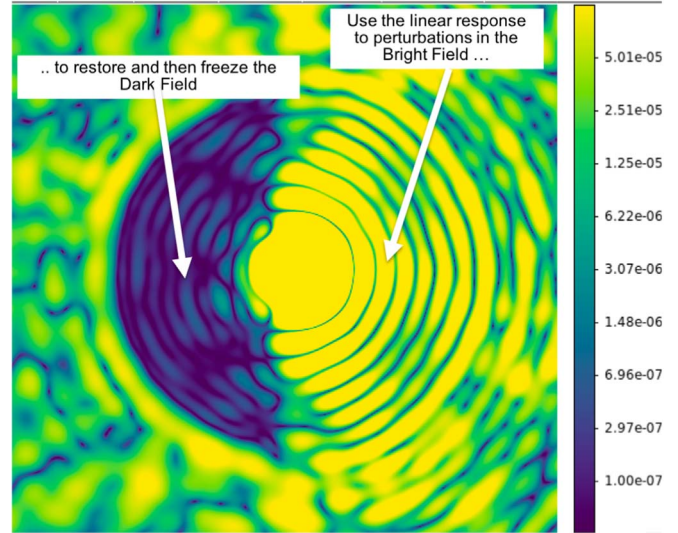


Figure 1. Schematic of Spatial Linear Field Dark Control obtained from simulated data for the ACE testbed. Bright, uncorrected regions with a contrast with respect to the peak intensity of $\sim 10^{-4}$ are used to stabilize a DH with a contrast of $\sim 10^{-7}$ – 10^{-8} .

(A color version of this figure is available in the online journal.)

LDFC does not require modulating the signal within the DH, it needs only a single focal plane image to restore the electric field to its initial state.

LDFC can be implemented in at least two ways. “Spatial” LDFC in a single band image, where a DH is created on one side of the image and stabilized by the BF on the opposite side (Miller et al. 2017) as shown in Figure 1. “Spectral” LDFC where the BF draws from pixels in out-of-band image slices at wavelengths bracketing the bandpass within which the DH is created (Guyon et al. 2017).

Miller et al. (2017) and Guyon et al. (2017) presented numerical simulations showing that an LDFC control loop should be able to hold static a DH at a 10^{-7} – 10^{-8} contrast level similar to that initially created using FPWFC methods. Miller et al. (2019) presented numerical simulations and early laboratory tests demonstrating LDFC coupled with the vector apodized phase plate coronagraph at 10^{-3} contrast between 4 and $11\lambda/D$; Currie et al. (2019b) presented preliminary results from the Ames Coronagraph Experiment (ACE) testbed showing that spatial LDFC may be successful at partially restoring a DH at 10^{-5} contrast in some cases. While encouraging, the tests were compromised by bright, static uncorrectable regions left on the focal plane images due to system internal reflection and non-ideal regularization of the control matrix used to map between changes in the focal plane and changes in the DM shape. Deeper contrasts (10^{-6} – 10^{-7}) are needed to test Spatial LDFC in regimes important for imaging exoplanets in reflected light from upcoming ground-based telescopes and space missions and better determine the limitations of LDFC.

¹⁷ Throughout, “corrected” means “corrected for aberrations using focal-plane wavefront sensing and control techniques.”

In this work, we present the first laboratory demonstration of Spatial LDFC at contrasts relevant for future imaging of exoplanets in reflected light, using the ACE testbed (Belikov et al. 2009). After briefly reviewing the premise of LDFC (Section 2), we describe our experimental setup for testing Spatial LDFC at ACE (Section 3) at contrasts relevant for imaging reflected-light planets but shallow enough that phase errors dominate the wavefront error budget (Shaklan & Green 2006; Pueyo & Kasdin 2007). Section 4 describes our results, where the LDFC control loop is used to largely restore DHs that are corrupted by a range of different perturbations and its performance is benchmarked against our implementation of a classical speckle nulling loop. The discussion (Section 5) details plans to further benchmark LDFC, testing its performance in regimes similar to those that will be faced with WFIRST-CGI, and sketches ways to implement a version of LDFC with WFIRST-CGI and future ground-based telescopes.

2. LDFC Background

LDFC theory was first described in Miller et al. (2017). The premise of LDFC is that perturbations in the pupil plane induce a response in the electric field in both the corrected, deep-contrast regions of the focal plane (the “dark field”; DF) and uncorrected, shallow-contrast regions (the “bright field”; BF). For spatial LDFC, this premise is generally true if phase errors dominate the wavefront error budget, as they produce aberrations in both the DF and BF regions (e.g., a sine wave perturbation on a DM producing a pair of speckles).¹⁸ This perturbation is small compared to the bright field intensity; the response to changes in the bright field is then linear, not quadratic. Given an influence function (e.g., a response matrix) that describes the mapping between the DM shape and changes in the bright field (with respect to its unperturbed state), one can find a unique solution to the change in DM shape that restores both the unperturbed bright field and dark field.

Briefly, the electrical field in focal plane at a given time t can be described as the sum of the incident electric field E_o established by focal-plane wavefront sensing techniques and a small change in complex amplitude due to a small wavefront error in a conjugate plane, E_1 , that corrupts the DH and could be corrected by the DM:

$$E_t \approx E_o + E_1. \quad (1)$$

The intensity in the focal plane, $I_t = |E_t|^2$, is then comprised of three terms. These are the intensity due to the initial electric field, the intensity due to changes in the electric field due to the wavefront error, E_1 , and the inner product between the two

electric field components:

$$|I_t| \approx |E_o|^2 + |E_1|^2 + 2\langle E_o, E_1 \rangle. \quad (2)$$

Within the dark field at time t , $|E_1|^2$ dominates, as the initial electric field component E_o is small. However, E_o is primarily responsible for the intensity distribution in the bright, uncorrected region: $|E_o|^2 \gg |E_1|^2$ and $2\langle E_o, E_1 \rangle \gg |E_1|^2$. Therefore, the change in the focal plane intensity I between time 0 and t in the BF is a linear function of the change in complex amplitude induced by changes in the electric field due to the wavefront error: $\Delta I = I_t - I_o \approx 2\langle E_o, E_1 \rangle$.

By (1) measuring changes in the bright field intensity between time t_o when the DH is first established and time t where it is corrupted and (2) constructing an influence function mapping between DM shape and focal plane intensity, we can then determine the set of DM actuator offsets that restore both the initial bright field and initial dark field corrupted by phase errors.

We adopt a system response matrix, RM, with dimensions of n bright field pixels by m actuators. The RM links together changes in DM shape Δu_t to changes in the bright field intensity distribution: $\Delta I_{DM,t} = RM \Delta u_t$. Actuator offsets Δu_t required to drive the dark field back to its original state at time t are then equal to the pseudo-inverse of RM (i.e., the “control matrix,” CM) multiplied by the change in the bright field, ΔI_{BF} :

$$\Delta u_t = -(RM^T RM)^{-1} RM^T \Delta I_{t,BF}. \quad (3)$$

LDFC has two potential key advantages over DM probing methods like EFC and speckle nulling, which use measurements of the DH directly for sensing and control. First, the signal within the photon-rich (uncorrected) bright field is larger than the (corrected) dark field and is not impacted by camera readout noise. Thus, for extremely deep-contrast DHs where the residual DH signal is photon starved, LDFC provides a higher signal-to-noise measurement of the DM shape needed to maintain/freeze the DH initial state.

Second, LDFC is a differential WFC technique. Once the CM for LDFC is determined, LDFC requires a single focal plane measurement to determine the change in DM shape that will restore the DH. In comparison, methods like EFC and speckle nulling rely on DM probing to determine the change in DM shape that will eliminate perturbations within the DH. Probing requires introducing perturbations in the pupil plane to determine the phase of speckles: e.g., for our implementation of classical speckle nulling, 4–6 probes must be introduced to solve for the speckle phase. Thus, even if the same number of iterations allow LDFC and methods like EFC/speckle nulling to restore the DH, the duty cycle for LDFC could be significantly shorter.

3. LDFC Experiments

We conducted tests of LDFC using the ACE laboratory at NASA-Ames Research Center in four separate experiments

¹⁸ Section 5 discusses the applicability and possible null space of LDFC in an ultra-deep contrast regime where amplitude errors become important.

Table 1
Experiment Log

Experiment Number	Date	Dark Field Size	Bright Field Size	Starting DH Contrast	Aberrations
1	2019 Sep 19	1.6–5.1 λ/D	1.4–5.1 λ/D	6.50×10^{-7}	single speckle
2	2019 Dec 23	1.6–5.1 λ/D	1.6–5.1 λ/D	5.97×10^{-7}	two speckles
3	2019 Jan 12	1.65–5.2 λ/D	1.55–5.2 λ/D	6.85×10^{-7}	low spatial frequency
4	2019 Jan 25	1.65–5.2 λ/D	1.65–5.2 λ/D	4.97×10^{-7}	complex/three speckles

Note. Starting DH Contrast refers to the average intensity within the DH with respect to the peak signal from the laser source. The average intensity over the (smaller) scoring regions for Experiments #2–4 is comparable.

between 2019 September and 2020 January (Table 1) at contrast levels shallow enough that phase errors are expected to dominate but deep enough to be relevant for future ground and space high-contrast imaging.

Our specific experiment milestone was as follows:

1. For a DH at a starting raw contrast of $\approx 10^{-6}$ that is degraded by at least a factor of 10 by injected phase perturbations over at least a region with an area of $\sim 10 (\lambda/D)^2$, demonstrate that (1) spatial LDFC can yield at least a $10\times$ gain in DH contrast and thus largely restore the DH and (2) hold this gain for over 100 iterations.
2. Achieve at least three successful demonstrations of achievements (1) and (2).

3.1. Laboratory Setup

The testbed uses a laser centered on 635 nm as a monochromatic light source. To limit file size and improve the speed of the WFC loop, we read out focal-plane images in 700×700 or 500×500 subarrays. The $1\lambda/D$ full-width-at-half-maximum point-spread function (PSF) size measured ~ 32 pixels.

For each experiment, satellite speckles were used to determine the conversion factor between counts and contrast with respect to the peak of an unocculted PSF. We used the PIAA coronagraph to suppress scattered starlight (Guyon 2003; Guyon et al. 2010) and a circular occulting spot of $\sim 1\lambda/D$ radius to yield a full 360° spatial coverage. To achieve an initial flat wavefront at the pupil plane, we use an implementation of the Gerchberg–Saxton method, which solves for the flat DM shape using a sequence of random pupil plane phase probes (Pluzhnik et al. 2017).

We used a classical speckle nulling control loop as implemented in previous ACE testbed experiments (e.g., Belikov et al. 2012) to correct for up to 81 speckles at a time. For each iteration of speckle nulling, we issue on average 10 DM commands: 7 to determine the phase of the speckles and 3 to determine amplitude.

The speckle nulling loop created a one sided, C-shaped DH extending from an inner working angle of $1.5\text{--}1.6\lambda/D$ to an outer working angle of $5.1\text{--}5.2\lambda/D$. The average contrast within the

DH measured between 4.97×10^{-7} and 6.85×10^{-7} depending on the experiment. In units of contrast, the approximate read-noise level of the detector was $\sim 5 \times 10^{-7}$ for the September and December experiments and a factor of 2 lower for the January experiments due to a factor of ≈ 10 longer exposures for the latter. Assuming a reasonable gain from post-processing (e.g., $30\text{--}50\times$), these raw contrasts are similar to the performance needed to detect Jovian planets at ~ 1 au in reflected light around nearby stars.

3.2. LDFC Matrix Setup and Closed-loop Implementation

To calculate the Spatial LDFC response matrix (RM), we perturbed each of the m actuators by a series of small amplitude pokes, 1 and 2, which are performed sequentially and have opposite signs (positive and negative). We then recorded the intensity I over n BF pixels. Each of the pokes have a fixed amplitude of $\text{ampl}_{\text{poke}}$. We combine results from two separate patterns— a and b —which differ by the order in which the positive/negative pokes are applied (i.e., $a = + - + -$, $b = + - - +$):

$$\text{RM}(n, m) = 0.5 * [(I_{a1} - I_{a2}) + (I_{b1} - I_{b2})] / (2 * \text{ampl}_{\text{poke}}). \quad (4)$$

The control matrix (CM) in a closed-loop implementation of LDFC is the pseudo-inverse of RM:

$$\text{CM} = (\text{RM}^T \text{RM})^{-1} \text{RM}^T. \quad (5)$$

Since (5) is usually ill-conditioned, we apply a truncated SVD regularization when computing it. Specifically, To compute CM, we decompose $(\text{RM}^T \text{RM})^{-1}$ into a matrix of eigenvectors V and a matrix of eigenvalues Λ , truncating Λ at mode k_{lim} before inverting to yield the CM: $\text{CM} = (V \Lambda^{-1} V^T)_{k < k_{\text{lim}}} \text{RM}^T$.

The normalized singular values of the RM covariance decline to $\sim 10^{-3}$ by $k = 200$ and flatten to 10^{-4} between $k = 250$ and $k = 1024$ (where the RM covariance would be at full-rank) (Figure 2). Inspection of the modal responses showed that signal at $k > 300$ was dominated by very high frequency pixel-to-pixel variations; at $k = 250$, the response was still

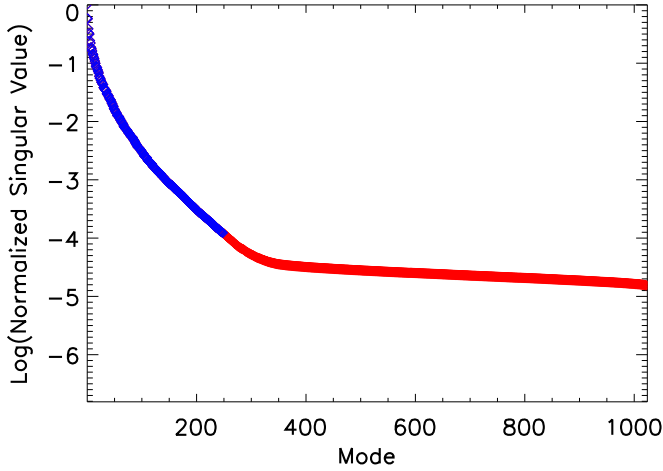


Figure 2. Singular values of the spatial LDFC response matrix, RM, for Experiment #4 (2020 January 25). Out of 1024 total modes, 250 modes (blue) were retained in the control matrix calculation, while higher modes (red) were discarded.

(A color version of this figure is available in the online journal.)

clearly dominated by spatially correlated signal (Figure 3). Thus, we set a modal cutoff to the CM at $k = 250$.

Our closed-loop implementation of LDFC multiplies the DM offset shape in the i -th iteration $\Delta u_{i,i}$ by a gain g and adds this value to the current DM shape: $DM_i = DM_{i-1} + \Delta u_{i,i} \times g$. We tested a range of gain values. For simplicity, we settled on $g = 0.25$ for all experiments, which provided a good balance between convergence speed and stability.

Early tests showed that the laser light source within ACE exhibited long-term centroid drift on a timescale comparable to our response matrix collection and closed-loop tests (see next section). Thus, the laser centroid position could be different between the response matrix calculation (i.e., the influence function) and its implementation in the spatial LDFC closed loop. To monitor and correct (within 1 pixel) the estimate of the centroid position, we introduced a single speckle into the DH prior to compare the centroid position at the start of the RM calculation and that during closed-loop tests, shifting the bright and dark field pixel masks by the offset between these two centroid measurements. Typical offsets were on the order of 2–4 pixels (0.06 – $0.12\lambda/D$); typical drift during closed-loop tests described below was on order of ~ 1 –2 pixels.

3.3. LDFC Experimental Setup

To test the efficacy of LDFC, for each experiment we introduce a perturbation in the pupil plane by slightly changing the DM shape from its map after the DH is created. This phase perturbation degrades the DH, and we use the LDFC control loop to restore it.

We introduced several different types of phase perturbations that result in a range of different focal plane aberrations

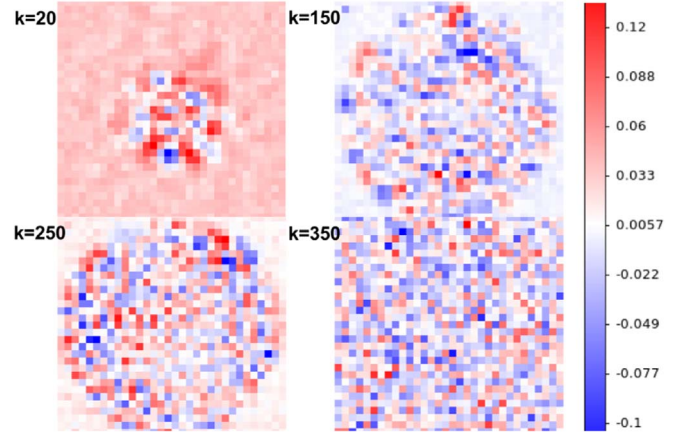


Figure 3. DM modes from the Control Matrix calculation for Experiment #4 (2020 January 25). For modes lower than $k \sim 250$, the response is confined to within a circular region that roughly match the coronagraph pupil. At modes higher than $k \sim 250$, the response varies at the pixel-to-pixel level.

(A color version of this figure is available in the online journal.)

(Table 1, rightmost column). Below, we describe these perturbations and list the date on which we performed these experiments.

1. A Single Speckle (2019 September 19)—We introduced a sine wave perturbation on the DM to yield a bright speckle with a peak contrast of $\sim 2 \times 10^{-4}$ into the DH.
2. A Pair of Speckles (2019 December 23)—We introduced sine wave perturbations on the DM to yield two bright speckles with peak contrasts of $\sim 5 \times 10^{-5}$ into the DH.
3. Low Spatial Frequency Aberration (2020 January 12)—To introduce this aberration, we poked a single actuator by an amplitude comparable to that used for our response matrix calculations, yielding a large region of the DH degraded to 10^{-5} contrast.
4. Complex Aberrations (2020 January 25)—To test for LDFC's ability to correct for more complex aberrations, we introduced a weighted, linear combination of sine wave perturbations on the DM, yielding three bright speckles in the DH, each with peak contrasts greater than 10^{-4} , along with with fainter aberrations at the $\sim 10^{-5}$ level.

For LDFC to be valuable, it must correct for speckles substantially brighter than the original DH average intensity, hold this correction for a large number of iterations, and exhibit an advantage (either in restored contrast or duty cycle) over standard DM probing methods like EFC or speckle nulling. For Experiment #1, we monitor the average intensity of the DH for over 100 iterations to assess whether the loop is stable. For Experiments #2–4, we compared LDFC's performance to that from speckle nulling. We used the same initial DM shape, the same (to within $\sim 5\%$) starting DH contrast, and the same perturbation. We compared the DH contrast over 100 iterations

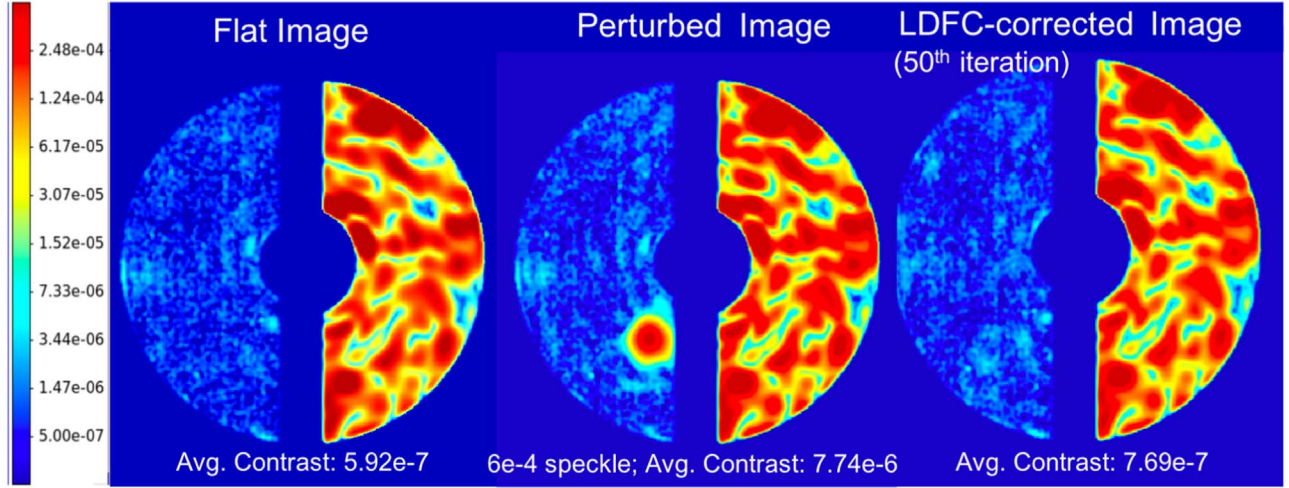


Figure 4. Sequence of focal plane camera images from our 2019 September 19/“Single Speckle” experiment showing that LDFC removes a bright speckle and drives the dark field back to an average contrast within 30% of its original value. The spatial scale for the dark (left) and bright (right) field regions is given in Table 1 and is roughly $1.5\text{--}5.1\lambda/D$; regions outside this range are masked out.

(A color version of this figure is available in the online journal.)

from speckle nulling, the number of iterations needed to restore the DH, and the number of DM shape changes needed.

To evaluate the efficacy of LDFC, for Experiments #2–4 we measured the contrast over scoring regions covering the locations of the perturbations in the dark field. For Experiments #2–3, we selected $10\lambda/D$ squared regions enclosing the two speckles and the peak intensity of the low spatial frequency perturbation, respectively. For Experiment #4, we selected the upper half of the DH (roughly $45\lambda/D$ squared). For these three experiments, the aberrations were adjusted to yield a factor of ~ 10 or more degradation in the average contrast over the scoring region.¹⁹

4. Results

4.1. Spatial LDFC DH Restoration

Figures 4 and 5 illustrate the ability of Spatial LDFC to restore a DH corrupted by a range of different phase-induced aberrations: one bright speckle, two speckles, a broad low spatial frequency aberration, and three speckles with fainter second order peaks. For the 2019 September, experiment, an initial (“flat”) image with an average DH contrast of $\sim 6 \times 10^{-7}$ is degraded by a single speckle with a peak contrast a factor of 1000 larger. The

average contrast over the entire DH increases by a factor of ~ 11 . Spatial LDFC immediately begins removing this speckle. LDFC achieves a restored DH with a contrast within $\sim 30\%$ of the original DH average intensity (righthand panel of Figures 4, 6). For the December and January experiments, the initial DH contrasts range between 5 and 6.9×10^{-7} over the entire DH and $(4.6\text{--}5.9) \times 10^{-7}$ within the relevant scoring regions (Figure 7). Aberrations degrade the DH by a factor of 4.6–13.7; within the scoring regions, the DH contrast is made 13–26 times brighter to $C \sim 7.2 \times 10^{-6}\text{--}1.2 \times 10^{-5}$.

Spatial LDFC then reduces the aberrated DH contrast by a factor of 3.7–9 over the entire field ($(7.4\text{--}9.5) \times 10^{-7}$; left two panels of Figure 5) and a factor of 10–13 over the scoring regions ($(7.4\text{--}9.3) \times 10^{-7}$; Figure 7). Over the entire DH region, LDFC reaches an average contrast within a factor of 1.2–1.4 of the pre-aberrated state. Within the scoring region, the restored average contrast is within a factor of 1.2–1.7 of its original value.

For Experiments 1–3, the initial aberration is (almost) perfectly removed by LDFC and most residual left by LDFC is largely confined to the edges of the DH region. We speculate that LDFC does not fully remove residual signal because (a) regions near the edge of the dark field/bright field are generally more difficult to correct and (b) the correction becomes “noisier” as average contrast approaches the read noise level. For Experiment #4, the initial aberration is largely removed but a faint residual core (~ 7 pixels in radius) of the brightest speckle remains after LDFC at a 10^{-5} level.²⁰

¹⁹ Key changes occurred after the September experiment. After September, multiple bad/weak actuators appeared on the ACE deformable mirror. In subsequent experiments, we masked these actuators in the initial creation of the DH and in the LDFC restoration of the DH. In the September experiment, the inner radius for the DH was smaller than the inner radius of the bright field. We found that this mismatch led to LDFC being unable to correct for perturbations closer to the optical axis. In subsequent experiments, we matched the inner radius for both regions. Finally, we coadded 10 times more images together in the December–January experiments to better illuminate the residual light within the DH.

²⁰ Section 5 discusses potential reasons why this residual signal and that in other experiments remain.

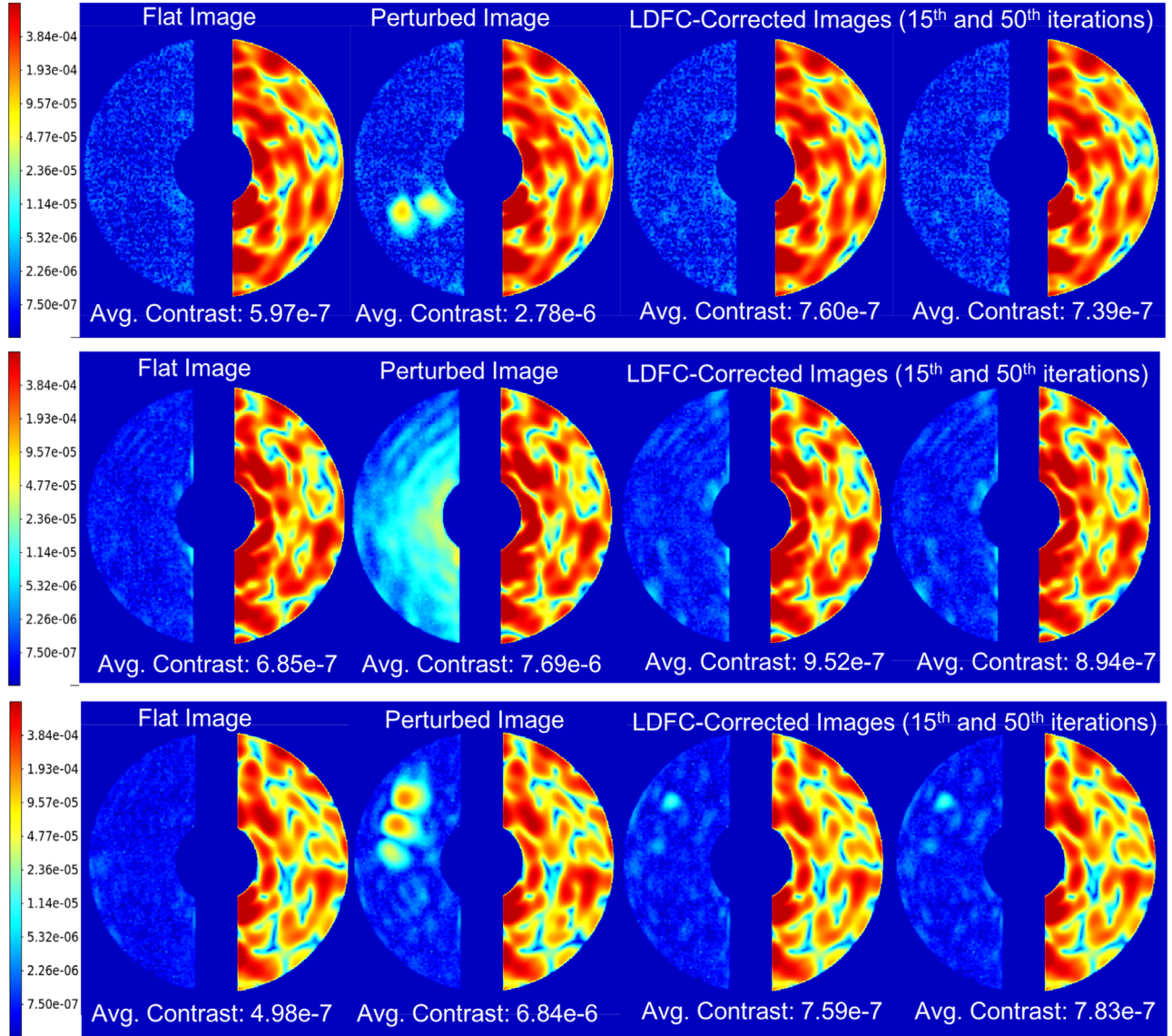


Figure 5. Sequence of images for LDFC experiments conducted on 2019 December 23/“Pair of Speckles” (top row), 2020 January 12/“Low Spatial Frequency Aberration” (middle row), and 2020 January 25/“Complex Aberration” experiments (bottom row). Shown are the initial camera image after the creation of a DH (left), the camera image after the introduction of a perturbation that degrades the DH (middle-left), and images after the 15th and 50th iteration of LDFC (middle-right, right). The spatial scale is the same as in Figure 4. Even for strong perturbations degrading contrast by over an order of magnitude, LDFC still returns the average intensity of the DH to within 20%–40% of its original value.

(A color version of this figure is available in the online journal.)

4.2. Stability of Spatial LDFC DH Correction and Comparison to Speckle Nulling

The Spatial LDFC-restored DH shows long-term stability. For the September experiment, the DH contrast converges after 18 iterations to a value of $8 \times 10^{-7} \pm 6.5 \times 10^{-8}$ for the next 105 iterations (Figure 6). The bright field stays constant within about the same fractional value: the average intensity fluctuations are expected given measured variations of the laser brightness with time ($\sim 5\%$). For the December and

January experiments (Figure 7), convergence to a final (largely) restored DH occurs within 5–10 iterations and stays constant within 10% for 110 iterations.

LDFC shows evidence for significantly improved efficiency compared to DM probing methods like speckle nulling. Speckle nulling is able to restore the DH to a contrast level $\sim (5\text{--}6) \times 10^{-7}$: 25%–40% lower than LDFC and comparable to the initial, unperturbed DH contrast. However, speckle nulling requires 20–70 iterations to reach its final contrast level

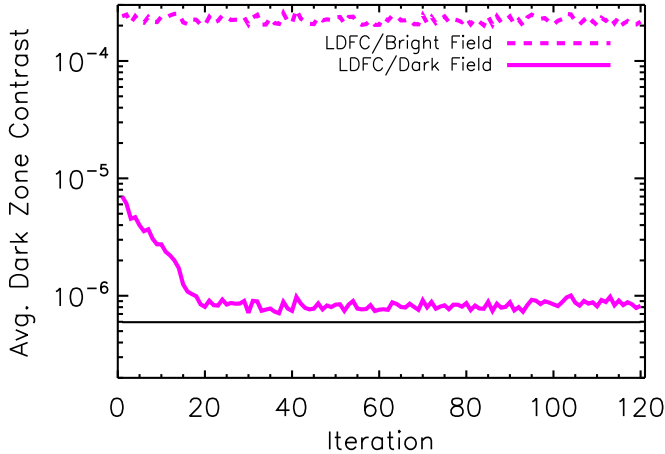


Figure 6. Analysis of our 2019 September 19/“Single Speckle” experiment. Contrast per iteration for LDFC for the perturbation introduced in Figure 4, showing that LDFC sustains a DH below 10^{-6} contrast for over 100 consecutive iterations.

(A color version of this figure is available in the online journal.)

(dashed–dotted blue lines). Reaching the contrast level achieved by LDFC requires a factor of 2–5 more iterations.

When analyzed in terms of DM commands, the efficiency advantage of LDFC is significantly larger. For each iteration, speckle nulling requires multiple DM probes in order to estimate the phase of residual speckles in the dark zone and estimate amplitude: 10 for our implementation. Speckle nulling requires a factor of 20–50 more DM commands to reach the contrasts achieved by LDFC. The advantage in duty cycle is particularly large for complex aberrations introduced into the focal plane (Experiment 4).

5. Discussion

5.1. Summary of Results and Implications

This study presents the first laboratory demonstrations of Spatial LDFC at contrast levels ($\sim 5 \times 10^{-7}$) and separations ($\sim 1.2\text{--}5.2\lambda/D$) approaching the raw performance needed to image some Jovian planets in reflected light around the nearest Sun-like stars with space-borne coronagraphic instruments like WFIRST-CGI and with ELTs around low-mass stars. In four experiments conducted with the ACE testbed, we introduced a range of different phase perturbations that degraded the average intensity of the DH ($a \geq (10\lambda/D)^2$ scoring area within the DH) by a factor of 5–10 (13–26). Spatial LDFC restores the average intensity of the DH to within a factor of 1.2–1.4 of its original contrast. In the scoring region focused on the perturbations, Spatial LDFC converges to within a factor of 1.2–1.7 of the original DH contrast. Spatial LDFC maintains the average DH contrast for over 100 iterations.

The Spatial LDFC experiments demonstrate significant potential advantages for maintaining a DH over methods that use DM probing to directly remove aberrations in the DH. When presented with the same aberrations, speckle nulling is able to achieve 25%–40% deeper contrasts than LDFC. However, speckle nulling requires a factor of 2–5 more iterations to match Spatial LDFC’s performance. As speckle nulling requires multiple modulations per iteration to estimate the phase of residual speckles in the DH, the duty cycle advantage for LDFC in terms of DM commands is substantial: a factor of 20–50 in our experiments.

LDFC may provide a promising path forward to maintain DHs without relying on DM modulation and probing, especially if its small performance gap compared to probing techniques is closed and if possible null space can be mitigated. The far shorter duty cycle offered by LDFC improves the efficiency of high-contrast imaging observations. By construction, LDFC drives the DH back to its initial state, which should improve the temporal correlation of speckles, while the LDFC loop is in operation. A shorter duty cycle and increased DH stability should substantially improve our ability to image mature solar system-like planets in reflected light over the next two decades.

5.2. Experiment Drawbacks and Null Space with Spatial LDFC

In our experiments, Spatial LDFC’s main drawback is that it converges to a DH contrast a factor of 1.2–1.7 higher than in the pre-aberrated state. Experimental conditions may account for much of this performance gap. For example, laser centroid drift during the RM calculation may compromise the accuracy of our influence function for LDFC. Drift during the closed-loop tests themselves likewise limits the accuracy of our correction. Instability in the laser power on the few percent level may limit accuracy as the average DH contrast approaches the initial, pre-aberrated state. The G -matrix encoding relationship between DM pokes and complex amplitudes for EFC may change with time, and similarly the RM for LDFC degrades with time. Weak/bad actuators on the DM not currently flagged may lead to a poor influence function determination and impede convergence.

Some of the aberrations degrading the DH may produce intensity variations at/near lowest-flux regions of the bright field may lie also in a quadratic response regime. A region of the bright field in the quadratic response regime would preclude identifying a unique DM shape that could be applied to restore its initial state and that of the dark field. This is a particularly relevant possibility for the residual speckle core left in Experiment #4, as bright field region 180° from that speckle is at a local minimum in flux.

Laser drift can be better corrected by monitoring the centroid position during the RM calculation and by improving our loop

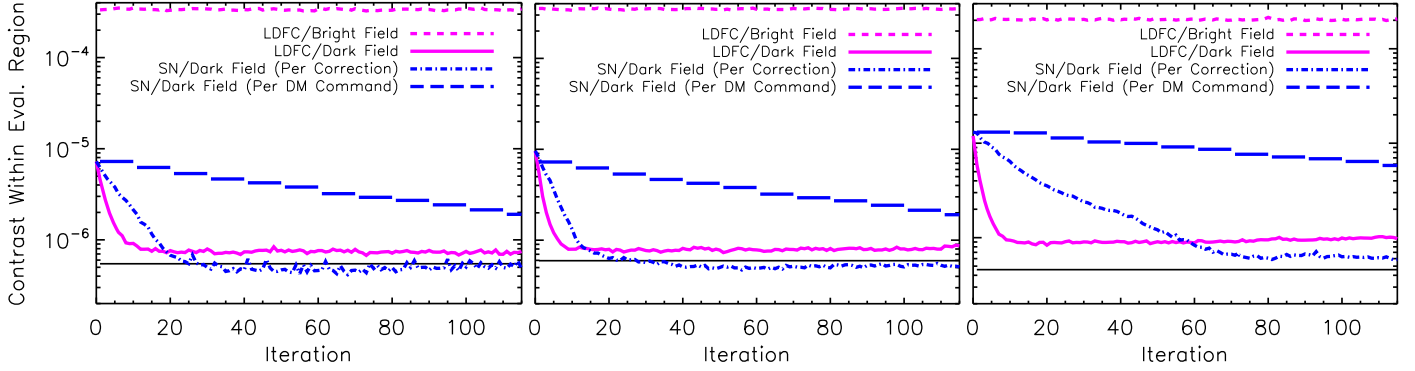


Figure 7. Contrast per iteration for the 2019 December 23/“Pair of Speckles” (left), 2020 January 12/“Low Spatial Frequency Aberration” (middle), and 2020 January 25/“Complex Aberration” (right) experiments for LDFC compared to performance of the speckle nulling algorithm used to create the DH. Horizontal black lines denote the initial average contrast within evaluation region before a perturbation is introduced to degrade the DH by a factor of 10–12. Within the DH, LDFC (solid magenta line) converges to within 20%–40% contrast twice as fast as deformable mirror probing with speckle nulling (blue dotted–dashed line) and with a factor of 20 or fewer deformable mirror commands (blue long-dashed line).

(A color version of this figure is available in the online journal.)

speed. Better regularization can limit the impact of laser instability. Future Spatial LDFC experiments at ACE will be conducted with a repaired DM or a replacement free of bad/dead actuators and with a more efficient loop to reduce the impact of system RM evolution.

A key concern for future progress with Spatial LDFC is the existence of null space, where a given pupil-plane perturbation aberrates the dark field but produces a negligible change in the bright field. Null space is expected to include a combination of amplitude and phase errors, which can create single-side speckles. By construction, our experiments only demonstrated spatial LDFC’s ability to remove phase errors that be represented by a linear combination of DM pokes (e.g., not perturbations with a spatial frequency higher than the DM pitch). More importantly, we did not, in this experiment, introduce amplitude errors in the pupil plane. Amplitude errors can result from reflectivity variations in system optics and phase-induced errors due to out of plane optics. Amplitude errors are expected to be equally important at raw contrasts in the range of 10^{-7} – 10^{-9} or below (e.g., Shaklan & Green 2006; Pueyo & Kasdin 2007; Bailey et al. 2018; J. Krist. 2020, private communication).

Null space can be addressed in the following ways. To partially compensate for null space for Spatial LDFC, the bright field mask could be adjusted, adding pixels exterior to but on the same side as the dark field, to be sensitive to at least some amplitude errors. It may be possible to treat amplitude and high spatial frequency phase perturbations by solving for an aberration map informed by a regression procedure. Constructing such a map requires quantitative modeling of the DM and coronagraph optical train and will be the subject of future work in simulations and on the ACE testbed. Finally, spectral LDFC (Guyon et al. 2017) utilizing out-of-band measurements over the same focal plane region for the bright and dark fields,

instead of different regions as in spatial LDFC, should be sensitive to both phase and amplitude aberrations provided that the main wavefront change is due to optical path difference in/near the pupil plane (where largest optics are). Improvements in the experimental setup for LDFC will enable a better tests of the method’s fundamental limits. Masking of lower-flux pixels with the bright field can focus LDFC on focal plane regions responding linearly to perturbations.

5.3. Future Tests of LDFC

Future experiments at the ACE testbed will further mature Spatial LDFC. Realistic aberrations (e.g., linear combination of Zernike modes) introduced mimicking those expected in flight for missions like WFIRST-CGI may provide a better practical test of Spatial LDFC. Our tests focus on sudden introductions of large-intensity perturbations into the dark field. An alternate test where smaller perturbations are periodically introduced and then corrected may better simulate closed-loop operations. Our experiments were conducted with the residual DH signal is well illuminated. “Blind” tests—where the DH residual intensity is comparable to the detector noise level over the WFS sampling time—can better assess LDFC’s advantage over DM probing techniques in the (dark field) photon-starved regime. Adopting more advanced focal-plane wavefront sensing techniques such as EFC, Kalman filtering, or variants that optimize DM probing and integration time (Groff & Kasdin 2013; Groff et al. 2016; Sun et al. 2020) instead of speckle nulling may provide a more robust assessment of LDFC’s advantages to state-of-the-art DM probing FPWFC methods.

Upcoming/proposed NASA missions capable of imaging exoplanets in reflected light like WFIRST-CGI, HabEx, and LUVOIR require sustained raw contrasts of 10^{-9} – 10^{-10} . Vacuum chamber experiments on the High-Contrast Imaging

Testbed at the Jet Propulsion Laboratory will provide a first test of LDFC’s efficacy at these extreme contrast regimes. For these tests, we will employ Spectral LDFC (Guyon et al. 2017), where out-of-band focal-plane images at wavelengths bracketing that of the main science bandpass will be needed to restore and freeze the DH. Typical exposures for these missions will be several to tens of hours. A key milestone then will be to demonstrate stability at $<10^{-9}$ – 10^{-10} contrast for tens of hours.

5.4. Practical Implementation of LDFC with WFIRST-CGI and ELTs

For implementation of Spatial LDFC either on the ground or (especially) in space, a key challenge will be the extremely high dynamic range required at the focal plane. The residual signal within the dark field must be illuminated and the bright field (10^3 – 10^4 times brighter) must be in the linear response regime. A neutral density filter covering the bright field or differential readout of the bright and dark regions could work around this problem.

Utilizing a version of LDFC may be possible with upcoming NASA missions, in particular WFIRST-CGI, but with some adjustments. WFIRST-CGI uses two deformable mirrors to generate a 360° DH. Nominally, Spatial LDFC would be at-best modestly effective for this setup as regions opposite a one-sided DH sample the same spatial scale, while regions exterior to the dark field sample a different scale and are not necessarily fully sensitive to the same focal-plane aberrations.

To compensate for such a setup and still utilize Spatial LDFC, one possibility is to simply create a one-sided DH and use the opposite side for wavefront sensing. As WFIRST-CGI’s technical demonstrations and foreseeable, subsequent science observations would focus on previously identified exoplanets with known positions (e.g., Greco & Burrows 2015), the DH region could be chosen beforehand with only a modest increase in the contrast requirements due to finite element corrections (Mawet et al. 2014).

The descope of the WFIRST-CGI integral field spectrograph prevents the utilization of Spectral LDFC as originally conceived of in Guyon et al. (2017); simultaneous, out-of-band broadband filter observations at wavelengths bracketing that of a science observation likewise are not possible. However, an “open loop” version of Spectral LDFC could be adopted, consisting of periodic images in out-of-band filters to “touch up” the wavefront correction. While less efficient than standard Spectral LDFC, the duty cycle for this method would be far smaller than the nominal strategy of slewing back to a PSF reference star to reestablish the DH. Spectral LDFC samples the same region of the image plane, in and out of band. As the chief challenge with any flavor of LDFC going forward is null space between the dark field and bright field dominated by amplitude and phase-induced amplitude errors, spectral

LDFC could potentially circumvent null space limitations of Spatial LDFC.

Utilization of LDFC with ELTs should be more straightforward. For instance, the Planetary Systems Imager on the Thirty Meter Telescope envisions high-contrast imaging observations with an integral field spectrograph that covers 0.6 – $1.8\ \mu\text{m}$ (Fitzgerald et al. 2019). For either a one-sided DH or a coronagraph yielding a deep correction over a small (e.g., 10%) bandpass, a version of LDFC could be employed. At raw contrasts needed to image Earth-like planets around nearby low-mass stars (10^{-6} at $1\ \mu\text{m}$), phase errors still dominate the wavefront error budget (Guyon et al. 2018).

A key challenge for the ground will be to demonstrate that the LDFC loop can converge significantly faster than the coherence time of atmospheric speckles: $t_0 \sim 5$ – 10 ms, even for the most high-contrast imaging-friendly site, Maunakea. To mature LDFC for these purposes, we plan to implement it as a separate WFC loop with the Subaru Coronagraphic Extreme Adaptive Optics project (Jovanovic et al. 2015; Lozi et al. 2018; Currie et al. 2019a). Internal source tests with SCEAO using a turbulence simulator already show promise (K. Miller & S. Bos 2020, in preparation).

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